

# Erindale College

|                    |                                  |
|--------------------|----------------------------------|
| Assessment Period: | 2021 S2                          |
| Course:            | SPECIALIST METHODS               |
| Unit:              | Unit 4: Specialist Methods (1.0) |
| Accreditation:     | T                                |
| Year:              | 12                               |

## Unit Goals

- understand the concepts and techniques in calculus, probability and statistics
- solve problems in calculus, probability and statistics
- apply reasoning skills in calculus, probability and statistics
- interpret and evaluate mathematical and statistical information and ascertain the reasonableness of solutions to problems
- communicate their arguments and strategies when solving problems

## Content Description

### Topic 1: Simple Linear Regression

- investigate scatter plots of two variables
- apply simple linear regression of  $y$  on  $x$  ( $\hat{y} = bx + a$ ) using method of least squares, including Interpolation and Extrapolation  $b = \frac{S_{xy}}{S_x}$  and  $a = \bar{y} - b\bar{x}$ , where:  $S_{xy} = \sum xy - \frac{\sum x \sum y}{n}$  and

$$S_x = \sum x^2 - \frac{(\sum x)^2}{n}$$

- compute correlation coefficient (at least Pearson's Method) and coefficient of determination
- use technology to fit line of best fit eg Excel, Geogebra, Calculator etc
- use real-life data (possible sources are ABS or AIHW ( <http://www.aihw.gov.au/data/> ))
- differentiate between correlation and causation

### Topic 2: Discrete random variables

- **General discrete random variables:**
  - o understand the concepts of a discrete random variable and its associated probability function, and their use in modelling data
  - o use relative frequencies obtained from data to obtain point estimates of probabilities associated with a discrete random variable
  - o recognise uniform discrete random variables and use them to model random phenomena with equally likely outcomes
  - o examine examples of non-uniform discrete random variables, for example Poisson and Hypergeometric distribution
  - o recognise the mean or expected value of a discrete random variable as a measurement of centre, and evaluate it in simple cases
  - o recognise the variance and standard deviation of a discrete random variable as a measures of

spread, and evaluate them in simple cases

o calculate means and variances of linear combinations of random variables (e.g.

$$E(aX + b) = aE(X) + b, \sigma_{aX+c}^2 = a^2 \sigma_X^2 \text{ etc})$$

o use discrete random variables and associated probabilities to solve practical problems

• **Bernoulli distributions:**

o use a Bernoulli random variable as a model for two-outcome situations

o identify contexts suitable for modelling by Bernoulli random variables

o recognise the mean  $p$  and variance  $p(1 - p)$  of the Bernoulli distribution with parameter  $p$

o use Bernoulli random variables and associated probabilities to model data and solve practical problems.

• **Binomial distributions:**

o understand the concepts of Bernoulli trials and the concept of a binomial random variable as the number of 'successes' in  $n$  independent Bernoulli trials, with the same probability of success  $p$  in each trial

o identify contexts suitable for modelling by binomial random variables

o determine and use the probabilities  $P(X = r) = \binom{n}{r} p^r (1 - p)^{n-r}$  associated with the

binomial distribution with parameters  $n$  and  $p$ ; note the mean  $np$  and variance  $np(1 - p)$  of a binomial distribution

o use binomial distributions and associated probabilities to solve practical problems, such as Markov Chains

o model real-life data, drawing inferences from specific to general

### Topic 3: Continuous random variables and the normal distribution

• **General continuous random variables:**

o use relative frequencies and histograms obtained from data to estimate probabilities associated with a continuous random variable

o understand the concepts of a probability density function, cumulative distribution function, and probabilities associated with a continuous random variable given by integrals; examine simple types of continuous random variables and use them in appropriate contexts

o recognise the expected value, variance and standard deviation of a continuous random variable and evaluate them in simple cases

o understand the effects of linear changes of scale and origin on the mean and the standard deviation.

• **Normal distributions:**

o identify contexts such as naturally occurring variation that are suitable for modelling by normal random variables

o recognise features of the graph of the probability density function of the normal distribution with mean  $\mu$  and standard deviation  $\sigma$  and the use of the standard normal distribution

o calculate probabilities and quantiles associated with a given normal distribution using technology, and use these to solve practical problems

o calculate interval estimate of the mean (e.g. 95% confidence limits)

o use Normal approximation to Binomial Distribution for  $np > 5$  and  $nq > 5$ , taking into account correction for continuity

## Topic 4: Interval estimates for proportions

### Random sampling:

- o understand the concept of a random sample
- o discuss sources of bias in samples, and procedures to ensure randomness
- o use graphical displays of simulated data to investigate the variability of random samples from various types of distributions, including uniform, normal and Bernoulli

### • Sample proportions:

- o understand the concept of the sample proportion  $\hat{p}$  as a random variable whose value varies between samples, and the formulas for the mean  $p$  and standard deviation  $\sqrt{(p(1-p))/n}$  of the sample proportion  $\hat{p}$
- o examine the approximate normality of the distribution of  $\hat{p}$  for large samples
- o simulate repeated random sampling, for a variety of values of  $p$  and a range of sample sizes, to illustrate the distribution of  $\hat{p}$  and the approximate standard normality of  $\frac{\hat{p} - p}{\sqrt{(\hat{p}(1-\hat{p}))/n}}$  where the closeness of the approximation depends on both  $n$  and  $p$

### • Confidence intervals for proportions:

- o the concept of an interval estimate for a parameter associated with a random variable
- o use the approximate confidence interval  $\left(\hat{p} - z\sqrt{(\hat{p}(1-\hat{p}))/n}, \hat{p} + z\sqrt{(\hat{p}(1-\hat{p}))/n}\right)$  as an interval estimate for  $p$ , where  $z$  is the appropriate quantile for the standard normal distribution
- o define the approximate margin of error  $E = z\sqrt{(\hat{p}(1-\hat{p}))/n}$  and understand the trade-off between margin of error and level of confidence
- o use simulation to illustrate variations in confidence intervals between samples and to show that most but not all confidence intervals contain  $p$

## Assessment Tasks

| Name         | Due Date    | Weighting |
|--------------|-------------|-----------|
| Assignment 1 | 30 August   | 15%       |
| Test 1       | 3 September | 35%       |
| Assignment 2 | 8 November  | 15%       |
| Test 2       | 12 November | 35%       |

## School Assessment Information

### For penalties for late and non-submission of work

See [BSSS Policy and Procedure Manual 4.3.10](#) for further information.

### For academic integrity

See [BSSS Policy and Procedure Manual 4.3.12](#) for further information.

**For appeals processes**

See [BSSS Policy and Procedure Manual 7.2](#) for further information.

**For moderation procedures (internal and external)**

See [BSSS Policy and Procedure Manual 5](#) for further information.

**For meshing procedures**

See [BSSS Policy and Procedure Manual 5.4.1](#) for further information.

**For method of unit score calculation**

See [BSSS Policy and Procedure Manual 4.3.6.2](#) for further information.

**For procedures for calculating course scores**

See [BSSS Policy and Procedure Manual 4.3.13.2](#) for further information.

## Achievement Standards for SPECIALIST METHODS T - Year 12

|                                     | <i>A student who achieves an A grade typically</i>  | <i>A student who achieves a B grade typically</i>   | <i>A student who achieves a C grade typically</i>  | <i>A student who achieves a D grade typically</i>  | <i>A student who achieves an E grade typically</i>   |
|-------------------------------------|---|---|--|--|--|
| <b>Reasoning and Communications</b> | <ul style="list-style-type: none"> <li>represents some mathematical concepts in numerical, graphical and symbolic form in routine and non-routine problems in a variety of contexts</li> <li>communicates mathematical judgements and arguments in oral, written and/or multimodal forms, which are succinct and reasoned, using appropriate and accurate language</li> <li>evaluates the solutions to routine and non-routine problems in a variety of contexts</li> <li>evaluates methods and models for their strengths and limitations when developing solutions to routine and non-routine problems</li> <li>reflects with insight on their own thinking and that of others and evaluates planning, time management, use of appropriate strategies to work independently and collaboratively</li> <li>evaluates the potential of Mathematics to generate knowledge in the public good</li> </ul> | <ul style="list-style-type: none"> <li>represents mathematical concepts in numerical, graphical and symbolic form in routine and non-routine problems in a variety of contexts</li> <li>communicates mathematical judgements and arguments in oral, written and/or multimodal forms, which are clear and reasoned, using appropriate and accurate language</li> <li>analyses the solutions to routine and non-routine problems in some contexts</li> <li>analyses strengths and limitations of models used when developing solutions to routine and non-routine problems</li> <li>reflects on their own thinking and analyses planning, time management, use of appropriate strategies to work independently and collaboratively</li> <li>analyses the potential of Mathematics to generate knowledge in the public good</li> </ul> | <ul style="list-style-type: none"> <li>represents mathematical concepts in numerical, graphical and symbolic form in some routine and non-routine problems in some contexts</li> <li>communicates mathematical judgements and arguments in oral, written and/or multimodal forms, using appropriate and accurate language</li> <li>explains solutions to some routine and non-routine problems in some contexts</li> <li>explains strengths and limitations of models used when developing solutions to some routine and non-routine problems</li> <li>reflects on their own thinking and explains planning, time management, use of appropriate strategies to work independently and collaboratively</li> <li>explains the potential of Mathematics to generate knowledge in the public good</li> </ul> | <ul style="list-style-type: none"> <li>represents simple mathematical concepts in numerical, graphical or symbolic form in routine problems in structured contexts</li> <li>communicates simple mathematical judgements or arguments in oral, written and/or multimodal forms, with some use of appropriate language</li> <li>describes solutions to routine problems in limited contexts</li> <li>describes strengths or limitations of simple models when solving routine problems</li> <li>reflects on their own thinking with some reference to planning, time management, use of appropriate strategies to work independently and collaboratively</li> <li>describes the potential of Mathematics to generate knowledge in the public good</li> </ul> | <ul style="list-style-type: none"> <li>represents simple mathematical concepts in numerical, graphical or symbolic form in simple problems in structured contexts</li> <li>communicates simple mathematical information in oral, written and/or multimodal forms, with limited use of appropriate language</li> <li>identifies solutions to routine problems in structured contexts</li> <li>identifies strengths or limitations of simple models in relation to routine problems</li> <li>reflects on their own thinking with little or no reference to planning, time management, use of appropriate strategies to work independently and collaboratively</li> <li>identifies some ways in which Mathematics is used to generate knowledge in the public good</li> </ul> |
| <b>Concepts and Techniques</b>      | <ul style="list-style-type: none"> <li>critically and creatively applies mathematical concepts in a variety of complex contexts to routine and non-routine problems</li> <li>synthesises information to select and apply mathematical techniques to solve complex problems in a variety of contexts</li> <li>constructs, selects and applies mathematical models to a variety of contexts in routine and non-routine problems</li> <li>uses digital technologies efficiently to solve routine and non-routine problems in a variety of contexts</li> </ul>  | <ul style="list-style-type: none"> <li>critically applies mathematical concepts in a variety of contexts to routine and non-routine problems</li> <li>analyses information to select and apply mathematical techniques to solve routine and non-routine problems in a variety of contexts</li> <li>selects and applies mathematical models to routine and non-routine problems in a variety of contexts</li> <li>uses digital technologies effectively to solve routine and non-routine problems in a variety of contexts</li> </ul>  | <ul style="list-style-type: none"> <li>applies mathematical concepts in some contexts to routine and non-routine problems</li> <li>selects and applies mathematical techniques to solve routine and some non-routine problems in some contexts</li> <li>applies mathematical models to routine and non-routine problems in some contexts</li> <li>uses digital technologies appropriately to solve routine and non-routine problems in a variety of contexts</li> </ul>  | <ul style="list-style-type: none"> <li>applies simple mathematical concepts in limited contexts to routine problems</li> <li>applies simple mathematical techniques to solve routine problems in limited contexts</li> <li>applies simple mathematical models to routine problems in limited contexts</li> <li>uses digital technologies appropriately to solve routine problems in limited contexts</li> </ul>  | <ul style="list-style-type: none"> <li>applies simple mathematical concepts in structured contexts</li> <li>uses simple mathematical techniques to solve routine problems in structured contexts</li> <li>demonstrates limited familiarity with mathematical models to solve routine problems in structured contexts</li> <li>uses digital technologies to solve routine problems in structured contexts</li> </ul>  |